

**Is Your Mass Defective?**

1. How much energy is released during the reaction:  ${}^1_1H + {}^7_3Li \rightarrow 2\ {}^4_2He$

$$1.00783 + 7.016 \rightarrow 2(4.0026)$$

$$8.02383 \rightarrow 8.0052 \quad \Delta m = 0.01863u$$

$$E=mc^2 = 0.01863(931) = 17.34 \text{ MeV}$$

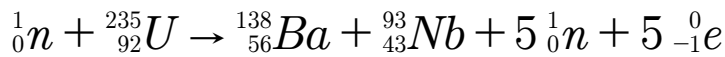
2. How much energy is released by each reaction of the following variety:  ${}^3_1H + {}^2_1H \rightarrow {}^4_2He + {}^1_0n$   
(One of the most promising fusion reactions!)

$$3.01604 + 2.0141 \rightarrow 4.0026 + 1.0087$$

$$5.03014 \rightarrow 5.0113 \quad \Delta m = 0.01863u$$

$$E=mc^2 = 0.01863(931) = 17.54 \text{ MeV}$$

Isotope/Species	Rest Mass
e	0.00055 u
n	1.0087 u
H-1	1.00783 u
H-2	2.0141 u
H-3	3.01604 u
He-4	4.0026 u
Li-7	7.016 u
Nb-93	92.906 u
Ba-138	137.905 u
U-235	235.0439 u



$$1.0087 + 235.0439 \rightarrow 137.905 + 92.906 + 5(1.0087) + 5(0.00055)$$

3. The above reaction shows the spontaneous fission decay of uranium into two daughter nuclei, 5 neutrons, and 5 beta particles. How much energy would be released when 1 atom on uranium is struck by one slow neutron? How much energy from 1 kg of uranium is possible?

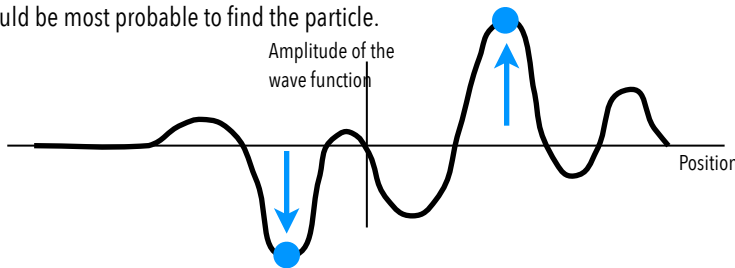
$$236.0526 \rightarrow 235.8573 \quad \Delta m = 0.19535u$$

$$E=mc^2 = 0.19535(931) = 181.87 \text{ MeV}$$

$$1000 \text{ g} \cdot 1\text{mol}/235.0439 \text{ g} \cdot 6.022 \cdot 10^{23} \text{ atoms/mol} = 2.562 \cdot 10^{24} \text{ atoms}$$

$$(2.562 \cdot 10^{24} \text{ atoms})(181.97 \text{ MeV/atom}) = 4.66 \cdot 10^{26} \text{ MeV} = 7.47 \cdot 10^{13} \text{ J}$$

4. deBroglie said that every particle behaves like a wave and vice-versa. Schrödinger said that every wave/particle has a wave function which shows the probability of the particle/wave being versus particular locations. Below is a graph of a wave function. Choose the **TWO** locations where it would be most probable to find the particle.



5. You have a sample of 120 grams of pure Ca-47 that undergoes  $\beta^-$  decay. Calcium-47 has a half life of 4.5 days. Draw a graph showing the grams of Ca-47 remaining as a function of time (Don't forget to label your axes). How much Ca-47 would be left after 63 days? What does the Ca-47 become? How much energy is released with every decay if the energy of the ejected neutrino is negligible?

$$63/4.5 = 14 \text{ halflives}$$

$$(1/2)^{14} = 6.1 \cdot 10^{-5} \text{ times the } 120 \text{ g} = 0.0073 \text{ g of Ca-47}$$



$$46.955 \rightarrow 0.00055 + 46.952 \quad \Delta m = 0.00245u$$

$$E=mc^2 = 0.00245(931) = 2.28 \text{ MeV}$$

